# T.E. (Mechanical) - 2012 Course Numerical Methods and Optimization [302047]

Code	Subject	Teaching Scheme (Weekly Load in hrs)		Examination Scheme (Marks)						
		Lect.	Tut	Pract.	Theory		TW	PR	OR	Total
					In Sem.	End Sem.				
302047	Numerical Methods and Optimization	4		2	30 (1 hr)	70 (2 hrs 30 min)		50		150

# **COURSE OBJECTIVES**

- 1 Recognize the difference between analytical and Numerical Methods.
- 2 Effectively use Numerical Techniques for solving complex Mechanical engineering Problems.
- 3 Prepare base for understanding engineering analysis software.
- 4 Develop logical sequencing for solution procedure and skills in soft computing.
- 5 Optimize the solution for different real life problems with available constraints.
- 6 Build the foundation for engineering research.

# **COURSE OUTCOMES**

- 1. Use appropriate Numerical Methods to solve complex mechanical engineering problems.
- 2. Formulate algorithms and programming.
- 3. Use Mathematical Solver.
- 4. Generate Solutions for real life problem using optimization techniques.
- 5. Analyze the research problem

# Unit – I Errors and Approximations

Types of Errors: Absolute, Relative, Algorithmic, Truncation, Round off Error, Error Propagation, Concept of convergence-relevance to numerical methods.

# Roots of Equation

Bisection Method, False position Method, Newton Raphson method and Successive approximation method.

### Unit – II Simultaneous Equations

Gauss Elimination Method, Partial pivoting, Gauss-Seidal method and Thomas algorithm for Tridiagonal Matrix

# Unit – III Optimization

Introduction to optimization, Classification, Constrained optimization: Graphical and Simplex method. One Dimensional unconstrained optimization: Newton's Method. Modern Optimization Techniques: Genetic Algorithm (GA), Simulated Annealing (SA).

# Unit –IV Curve Fitting & Interpolation

### **Curve** Fitting

Least square technique- Straight line, Power equation, Exponential equation and Quadratic equation.

# Interpolation

Lagrange's Interpolation, Newton's Forward interpolation, Hermit Interpolation, inverse interpolation.

### Unit – V Numerical Integration

Trapezoidal rule, Simpson's Rule (1/3<sup>rd</sup> and 3/8<sup>th</sup>), Gauss Quadrature 2 point and 3 point method. Double Integration: Trapezoidal rule, Simpson's 1/3<sup>rd</sup>Rule.

### Unit –VI Numerical Solutions of Differential Equations Ordinary Differential Equations [ODE]

Taylor series method, Euler Method, Modified Euler Method(Iterative), RungeKuttafourth order Method, Simultaneous equations using RungeKutta2nd order method.

### Partial Differential Equations [PDE]: Finite Difference methods

Introduction to finite difference method, PDEs- Parabolic explicit solution, Ellipticexplicit solution.

# (10 hrs)

# (06 hrs)

#### (06 hrs)

(10 hrs)

#### tion

(08 hrs)

(08 hrs)

# **Term-Work**

- 1. Program on Roots of Equation (Validation by suitable solver, all four compulsory)
  - a). Bisection Method, b. False position Method,
  - c). Newton Raphson method d. Successive approximation method
- 2. Program on Simultaneous Equations (Validation by suitable solver, all three compulsory)
  - a) Gauss Elimination Method,
  - b) Thomas algorithm for tridiagonal matrix,
  - c) Gauss-Seidal method.
- 3. Program on Numerical Integration(Validation by suitable solver, all four compulsory)
  - a) Trapezoidal rule,
  - b) Simpson's Rules  $(1/3^{rd}, 3/8^{th})$  [In one program only]
  - c) Gauss Quadrature Method- 2 point, 3 point. [In one program only]
  - d) Double integration: Trapezoidal rule, Simpson's 1/3<sup>rd</sup>Rule.
- 4. Program on Curve Fitting using Least square technique (Validation by suitable solver, all four compulsory)
  - a) Straight line,
  - b) Power equation
  - c) Exponential equation
  - d) Quadratic equation
- 5. Program on Interpolation(Validation by suitable solver, all three compulsory)
  - a) Lagrange's Interpolation,
  - b) Newton's Forward interpolation,
  - c) Inverse interpolation
- 6. Program on ODE(Validation by suitable solver, all three compulsory)
  - a) Euler Method(Iterative),
  - b) Runge-Kutta Methods- fourth order,
  - c) Simultaneous equations.(Runge-Kutta 2nd order: One step only).
- 7. Program on PDE(Validation by suitable solver)
- 8. Theory assignment on Modern Optimization techniques.

### **GUIDELINES TO CONDUCT PRACTICAL EXAMINATION**

Any one program from each set A & B with flowchart and solver: Duration: 2 hrs.

- Set A: (Weightage 60 %) a). Simultaneous Equation. b). Partial Differential Equation c). Interpolation.
- **Set B:** (Weightage 40 %)
  - a). Roots of Equations. b). Curve Fitting. c). Ordinary Differential Equations. d). Integration

### **Text Books**

- 1. Steven C. Chapra, Raymond P. Canale, Numerical Methods for Engineers, 4/e, Tata McGraw Hill Editions
- 2. Dr. B. S. Garewal, Numerical Methods in Engineering and Science, Khanna Publishers,.
- 3. Steven C. Chapra, Applied Numerical Methods with MATLAB for Engineers and Scientist, Tata Mc-GrawHill Publishing Co-Ltd
- 4. Rao V. Dukkipati, Applied Numerical Methods using Matlab, New Age International Publishers

### **Reference Books**

- 1. Gerald and Wheatley, Applied Numerical Analysis, Pearson Education Asia
- 2. E. Balagurusamy, Numerical Methods, Tata McGraw Hill
- 3. P. Thangaraj, Computer Oriented Numerical Methods, PHI
- 4. S. S. Sastry, Introductory Methods of Numerical Analysis, PHI.